

Advanced Model Checking  
 Summer term 2012

## – Series 7 –

Hand in on June 13 before the exercise class.

## Exercise 1

(3 points)

For the given function:

$$F(x_0, \dots, x_{n-1}, a_0, \dots, a_{k-1}) = x_{|a|}$$

where  $n = 2^k$ ,  $\forall i \in 0 \dots n-1 : x_i = 0 \vee x_i = 1$ ,  $\forall j \in 0 \dots k-1 : a_j = 0 \vee a_j = 1$  and  $|a| = \sum_{j=0}^{k-1} a_j 2^j$ , provide two ROBDDs, considering the following two variable orderings:

$$a_0, \dots, a_{k-1}, x_0, \dots, x_{n-1}$$

and

$$a_0, x_0, \dots, a_{k-1}, x_{k-1}, x_k, \dots, x_{n-1}$$

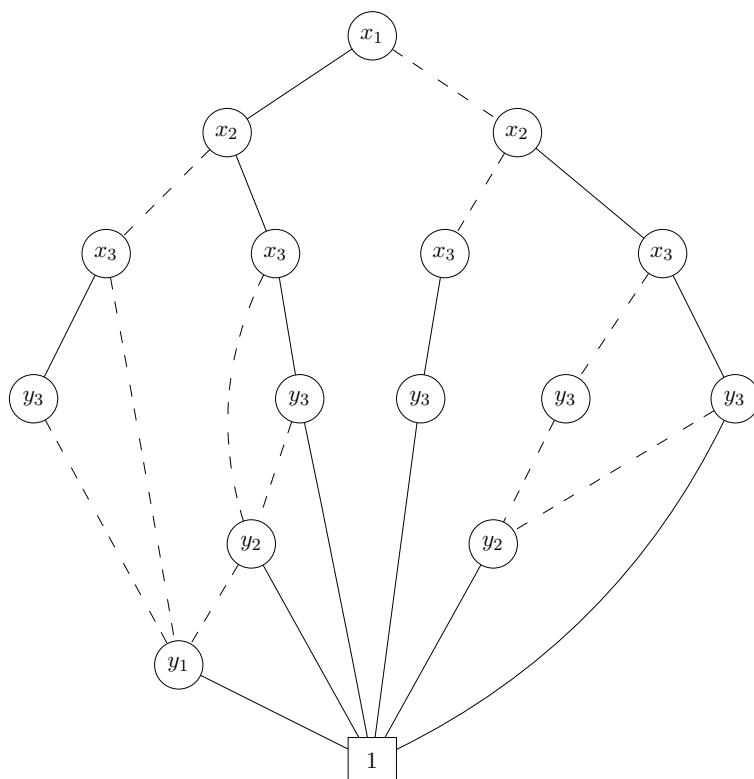
with  $k = 3$ .

## Exercise 2

(2 points)

Given an ROBDD as follows, determine the boolean function  $f(x_1, x_2, x_3, y_1, y_2, y_3)$  it represents.

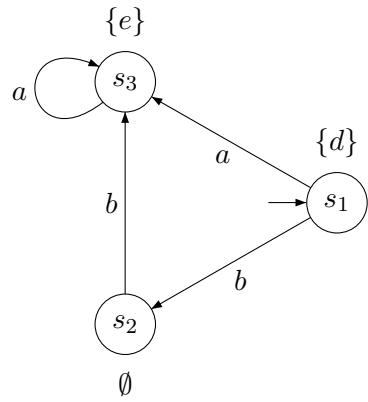
(Hint: first to find a better variable ordering)



**Exercise 3**

(2 points)

Given a transition system  $TS$  with actions as follows:

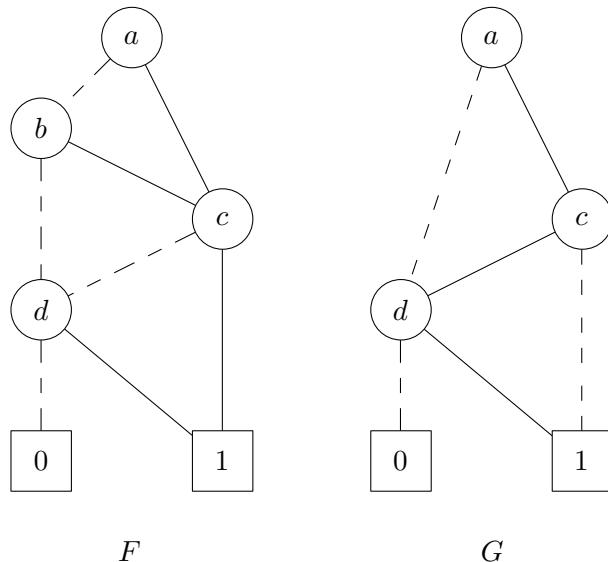


- Define how to obtain switching functions for this case and find a switching function for the above  $TS$ ;
- Encode the  $TS$  by a ROBDD.

**Exercise 4**

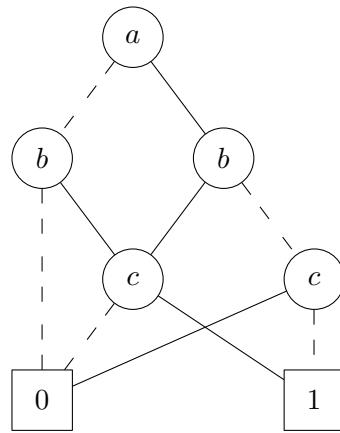
(3 points)

- Compute  $F \vee G$  for the following ROBDDs:



Provide the intermediate steps.

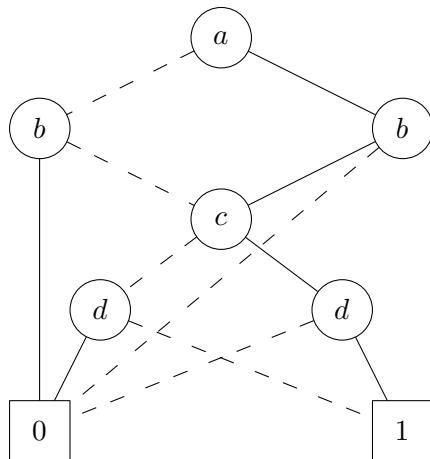
- Compute  $H|_{b=1}$ , given the ROBDD below:



$H$

Provide the intermediate steps.

c) Compute  $\exists a.(\exists d.f(a, b, c, d))$  in the form of ROBDD for the  $f$  function defined by the ROBDD below:



Provide intermediate steps.