

Compiler Construction

Lecture 16: Semantic Analysis IV & Code Generation I

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Summer semester 2008

- 1 Repetition: Attribute Evaluation
- 2 Simultaneous Parsing and Attribute Evaluation
- 3 Generation of Intermediate Code
- 4 The Example Programming Language EPL

Attribute Evaluation Methods

Given:

- (strongly) noncircular attribute grammar

$$\mathfrak{A} = \langle G, E, V \rangle \in AG$$

- syntax tree t of G

- valuation $v : Syn_{\Sigma} \rightarrow V$ where

$$Syn_{\Sigma} := \{ \alpha.k \mid k \text{ labelled by } a \in \Sigma, \alpha \in \text{syn}(a) \} \subseteq Var_t$$

Goal: extend v to (partial) **solution** $v : Var_t \rightarrow V$

Methods:

- ① **Topological sorting** of D_t :

- ① start with attribute variables which depend at most on synthesized attributes of terminals
- ② proceed by successive substitution

- ② **Recursive functions** (for strongly noncircular AGs):

- ① for every $A \in N$ and $\alpha \in \text{syn}(A)$, define evaluation function $g_{A,\alpha}$ with the following parameters:

- the node of t where α has to be evaluated and
- all inherited attributes of A on which α (potentially) depends

- ② for every $\alpha \in \text{syn}(S)$, evaluate $g_{S,\alpha}(k_0)$ where k_0 denotes the root of t

- ③ Special cases: **S-attributed grammars** (yacc), **L-attributed grammars**

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In an L-attributed grammar, attribute dependencies on the right-hand sides of productions are only allowed to run **from left to right**.

Definition 16.1 (L-attributed grammar)

Let $\mathfrak{A} = \langle G, E, V \rangle \in AG$ such that, for every $\pi \in P$ and $\beta.i = f(\dots, \alpha.j, \dots) \in E_\pi$ with $\beta \in Inh$ and $\alpha \in Syn$, $j < i$. Then \mathfrak{A} is called an **L-attributed grammar** (notation: $\mathfrak{A} \in LAG$).

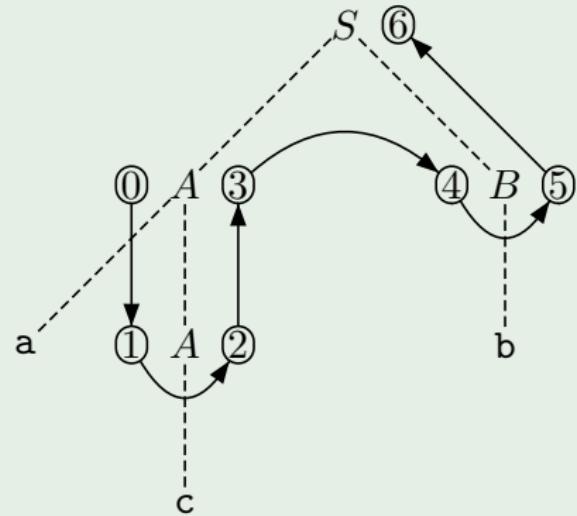
Corollary 16.2

Every $\mathfrak{A} \in LAG$ is noncircular.

Example 16.3

L-attributed grammar:

$$\begin{array}{ll} S \rightarrow AB & i.1 = 0 \\ & i.2 = s.1 + 1 \\ & s.0 = s.2 + 1 \\ A \rightarrow aA & i.2 = i.0 + 1 \\ & s.0 = s.2 + 1 \\ A \rightarrow c & s.0 = i.0 + 1 \\ B \rightarrow b & s.0 = i.0 + 1 \end{array}$$



Observation 1: the syntax tree of an L-attributed grammar can be attributed by a **depth-first, left-to-right tree traversal** with **two visits** to each node

- ① **top-down**: evaluation of **inherited** attributes
- ② **bottom-up**: evaluation of **synthesized** attributes

Observation 2: visit sequence fits nicely with **parsing**

- ① **top-down**: expansion steps
- ② **bottom-up**: reduction steps

Idea: extend LL parsing to support reduction steps, and integrate attribute evaluation

⇒ use **$LR(0)$** items as stack alphabet
and store values of attribute variables in parsing stack

Definition 16.4 (Parsing automaton with attribute evaluation)

Let $\mathfrak{A} = \langle G, E, V \rangle \in LAG$ with $G = \langle N, \Sigma, P, S \rangle \in LL(1)$. The **parsing automaton with attribute evaluation** of \mathfrak{A} is defined by the following components.

- **Input alphabet** Σ
- **Pushdown alphabet** $\Gamma := \bigcup_{\pi \in P \cup \{\rightarrow S\}} (LR(0)_\pi(G) \times Val_\pi)$ where
 - $LR(0)_\pi(G) := \{[A \rightarrow \delta_1 \cdot \delta_2] \mid \pi = A \rightarrow \delta_1 \delta_2\}$ and
 - $Val_\pi := \{v \mid v : Out_\pi \dashrightarrow V\}$
- **Configurations** $\Sigma^* \times \Gamma^*$
 - **initial configuration:** $(w, ([\rightarrow \cdot S], v_\emptyset))$
 - **final configurations:** $\{(\varepsilon, ([\rightarrow S \cdot], v)) \mid v \in Val_{\rightarrow S}\}$

Definition 16.4 (continued)

- **Transitions:**

expand: (evaluate inherited attributes of expanded symbol)

if $x \in \text{la}(B \rightarrow \delta')$, then

$$\begin{aligned} & (xw, ([A \rightarrow Y_1 \dots Y_{i-1} \cdot B\delta], v)\gamma) \\ \vdash & (xw, ([B \rightarrow \cdot\delta'], v'))([A \rightarrow Y_1 \dots Y_{i-1} \cdot B\delta], v)\gamma) \end{aligned}$$

where $v' := [\beta.0 \mapsto f(v(\alpha_1.i_1), \dots, v(\alpha_n.i_n))]$ for
 $\beta \in \text{inh}(B)$ and

$$\beta.i = f(\alpha_1.i_1, \dots, \alpha_n.i_n) \in E_{A \rightarrow Y_1 \dots Y_{i-1} B\delta}$$

match: $(aw, ([A \rightarrow \delta_1 \cdot a\delta_2], v)\gamma)$

$$\vdash (w, ([A \rightarrow \delta_1 a \cdot \delta_2], v)\gamma)$$

reduce: (evaluate synthesized attributes of reduced symbol)

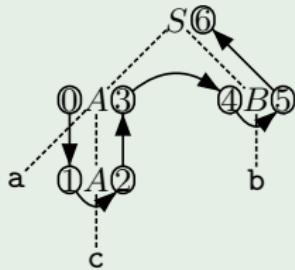
$$\begin{aligned} & (w, ([B \rightarrow \delta' \cdot], v'))([A \rightarrow Y_1 \dots Y_{i-1} \cdot B\delta], v)\gamma) \\ \vdash & (w, ([A \rightarrow Y_1 \dots Y_{i-1} B \cdot \delta], v'')\gamma) \end{aligned}$$

where $v'' := v[\alpha.i \mapsto f(v'(\alpha_1.i_1), \dots, v'(\alpha_n.i_n))]$ for
 $\alpha \in \text{syn}(B)$ and $\alpha.0 = f(\alpha_1.i_1, \dots, \alpha_n.i_n) \in E_{B \rightarrow \delta'}$

LL(1) Parsing with Attribute Evaluation III

Example 16.5 (cf. Example 16.3)

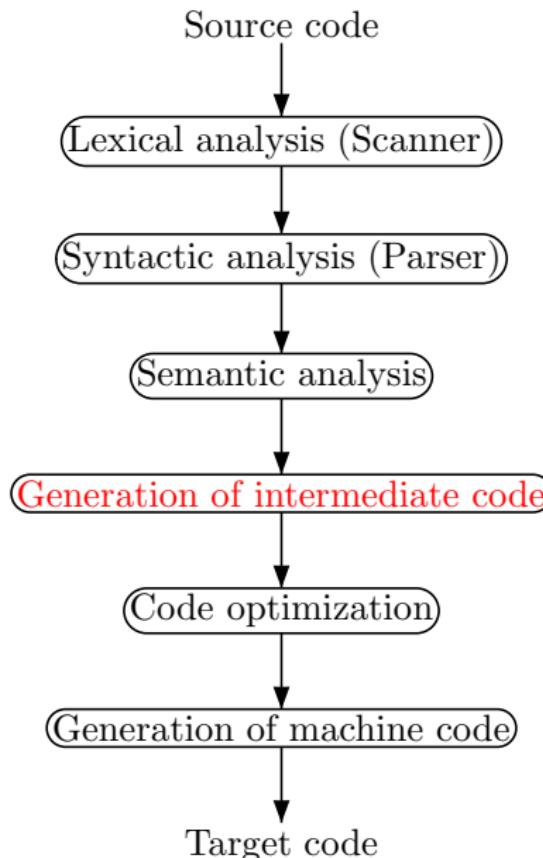
$S \rightarrow AB$
 $A \rightarrow aA$
 $A \rightarrow c$
 $B \rightarrow b$



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Conceptual Structure of a Compiler



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Modularization of Code Generation I

Splitting of code generation for programming language PL:

$$\text{PL} \xrightarrow{\text{trans}} \text{IC} \xrightarrow{\text{code}} \text{MC}$$

Frontend: trans generates **machine-independent intermediate code** (IC) for abstract (stack) machine

Backend: code generates **actual machine code** (MC)

Advantages: IC machine independent \Rightarrow

Portability: much easier to write IC compiler/interpreter for a new machine (as opposed to rewriting the whole compiler)

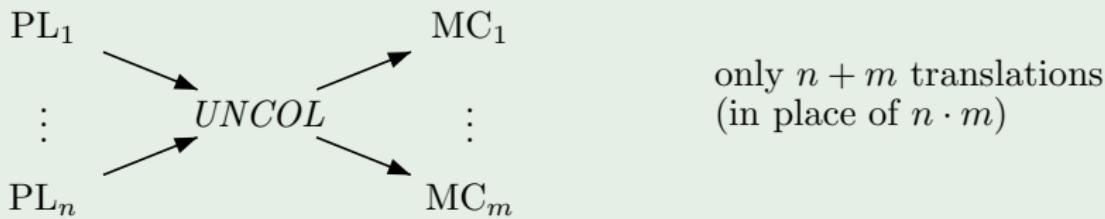
Fast compiler implementation: generating IC much easier than generating MC

Code size: IC programs usually smaller than corresponding MC programs

Code optimization: division into machine-independent and machine-dependent parts

Example 16.6

- ① UNiversal Computer-Oriented Language (UNCOL; ≈ 1960 ;
<http://en.wikipedia.org/wiki/UNCOL>):
universal intermediate language for compilers (never fully specified or implemented; too ambitious)



- ② Pascal's pseudocode (P-code; ≈ 1975 ;
http://en.wikipedia.org/wiki/P-Code_machine)
- ③ The Amsterdam Compiler Kit (TACK; since 1980;
<http://tack.sourceforge.net/>)
- ④ Java Virtual Machine (JVM; Sun;
http://en.wikipedia.org/wiki/Java_Virtual_Machine)
- ⑤ Common Intermediate Language (CIL; Microsoft;
http://en.wikipedia.org/wiki/Common_Intermediate_Language)

Structures in imperative programming languages:

(object-oriented, declarative [functional/logic]: see special courses)

- Basic data types and basic operations
- Static and dynamic data structures
- Expressions and assignments
- Control structures (sequences, branching statements, loops, ...)
- Procedures and functions
- Modularity: blocks, modules, and classes

Use of procedures and blocks:

- FORTRAN: non-recursive and non-nested procedures
 ⇒ **static** memory management (memory requirement determined at compile time)
- C: recursive and non-nested procedures
 ⇒ dynamic memory management using **runtime stack** (memory requirement only known at runtime), no static links
- Algol-like languages (Pascal, Modula): recursive and nested procedures
 ⇒ dynamic memory management using **runtime stack with static links**

Structures in machine code: (von Neumann/SISD)

Memory hierarchy: accumulators, registers, cache, main memory, background storage

Instruction types: arithmetic/Boolean/... operation, test/jump instruction, transfer instruction, I/O instruction, ...

Address modes: direct/indirect, absolute/relative, ...

Architectures: RISC (few [fast but simple] instructions, many registers), CISC (many [complex but slow] instructions, few registers)

Structures in intermediate code:

- **Data types and operations** like PL
- **Data stack** with basic operations
- **Jumping instructions** for control structures
- **Runtime stack** for blocks, procedures, and static data structures
- **Heap** for dynamic data structures

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Structures of EPL:

- Only integer and Boolean **values**
- Arithmetic and Boolean **expressions** with strict and non-strict semantics
- **Control structures**: sequence, branching, iteration
- Nested **blocks** and recursive **procedures** with local and global variables
(\Rightarrow dynamic memory management using runtime stack with static links)
- Procedure **parameters** and **data structures** later

Syntax of EPL

Definition 16.7 (Syntax of EPL)

The **syntax of EPL** is defined as follows:

$\mathbb{Z} : z$ (* z is an integer *)

$Ide : I$ (* I is an identifier *)

$AExp : A ::= z \mid I \mid A_1 + A_2 \mid \dots$

$BExp : B ::= A_1 < A_2 \mid \text{not } B \mid B_1 \text{ and } B_2 \mid B_1 \text{ or } B_2$

$Cmd : C ::= I := A \mid C_1; C_2 \mid \text{if } B \text{ then } C_1 \text{ else } C_2 \mid \text{while } B \text{ do } C \mid I()$

$Dcl : D ::= D_C \ D_V \ D_P$

$D_C ::= \varepsilon \mid \text{const } I_1 := z_1, \dots, I_n := z_n;$

$D_V ::= \varepsilon \mid \text{var } I_1, \dots, I_n;$

$D_P ::= \varepsilon \mid \text{proc } I_1; K_1; \dots; I_n; K_n;$

$Block : K ::= D \ C$

$Pgm : P ::= \text{in/out } I_1, \dots, I_n; K.$

- All identifiers in a declaration D have to be **different**.
- Every identifier occurring in the command C of a block D C must be **declared**
 - in D or
 - in the declaration list of a surrounding block.
- **Multiple declarations** of an identifier in different blocks are possible. Each usage in a command C refers to the “**innermost**” declaration.
- **Static scoping**: the usage of an identifier in the body of a called procedure refers to its declaration environment (and not to its calling environment).

Example 16.8

```
in/out x;  
  const c = 10;  
  var y;  
  proc P;  
    var y, z;  
    proc Q;  
      var x, z;  
      [... z := 1; P() ...]  
      [... P() ... R() ...]  
    proc R;  
      [... P() ...]  
      [... x := 0; P() ...] .
```

- “Innermost” principle
- Static scoping: body of P can refer to x, y, z
- Later declaration: call of R in P followed by declaration (in Pascal: **forward** declarations for one-pass compilation)