

REALIZABILITY

FOUNDATIONS OF THE UML

Lecture #7: Realizing

local choice MSGs

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- Recall: mapping a set of MSCs — possibly given by an MSG — onto a distributed implementation (an MPA)
- Basic results: characterization of sets of MSCs (in terms of their traces) that are realizable or even safely realizable
- Checking realizability for a finite set of MSCs is CONP-complete, whereas safe realizability can be checked in PTIME
- A necessary condition for MSGs — that may specify an infinite set of MSCs — for realizability is communication-closedness
- In fact, regular MSC languages are realizable by deterministic MPA, but unfortunately, checking whether an MSG yields such language, is undecidable.

REALIZATION OF LOCAL CHOICE MSG

- Characterizations of (safe) realizability are non-constructive, i.e., they allow to decide whether a set of MSGs is realizable but not how.
- For a limited number of cases, algorithms can be provided for obtaining realizations.
- For example, we (=t2) investigate the usage of learning algorithms; see our tool Smyle
- This lecture: an algorithm for the safe realizability of local choice MSGs, i.e.,

local choice algorithm deadlock free
MSG ~~~~~ MPA

RECALL: LOCAL CHOICE

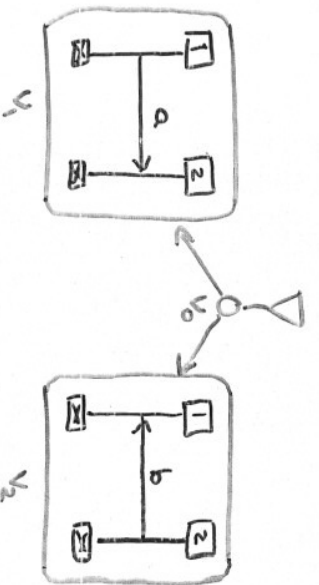
- e is a minimal event wrt. $<$ if $\neg (\exists e' \in E. e' < e)$
- Process p is active in MSC M if $E_p \neq \emptyset$
- p is active in path $\underbrace{y_1 y_2 \dots y_n}_{\pi}$ in MSG G if $\exists y_i \in \pi. p$ is active in $\underbrace{\lambda(y_i)}_{= \text{MSC of vertex } y_i}$
- MSG $G = (V, \rightarrow, v_0, F, \lambda)$ is local choice if
 - (1) $\exists$ active $p. \forall \pi \in \text{Paths}(v_0). \pi$ has a single minimal event e with $e \in F$
 - (2) $\forall$ branching vertex $v \in V. \exists$ active $p. \forall \pi \in \text{Paths}(v)$ with $v \rightarrow w. \pi$ has a single minimal event e with $e \in F_p$
- $v \in V$ is a branching vertex if



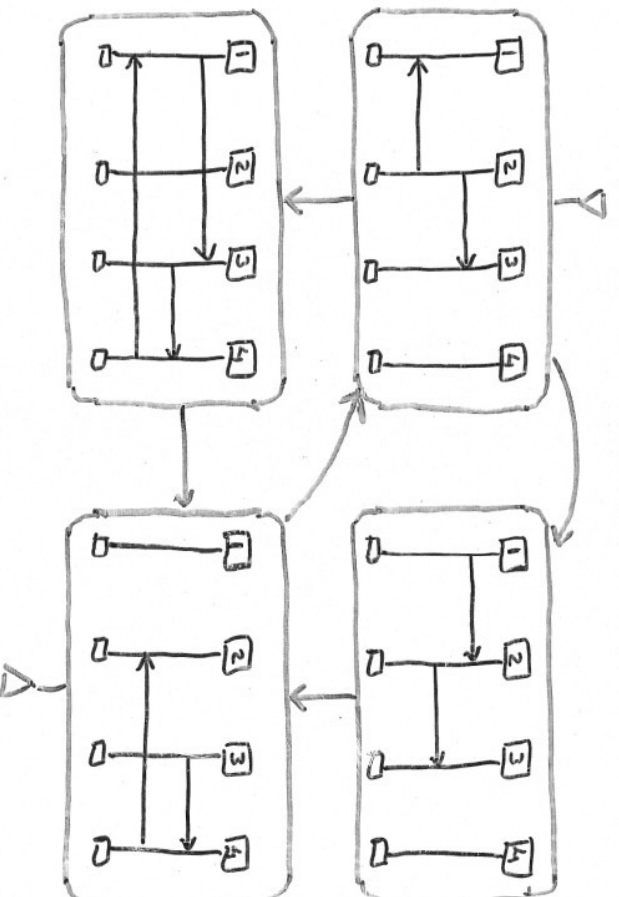
> 1 direct successor

≥ 1 direct successor

LOCAL CHOICE MSGs



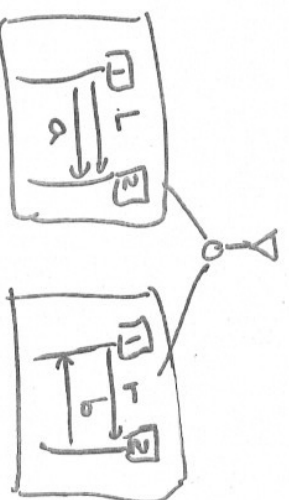
non local
choice



local choice

LOCAL CHOICE MSGs

- Checking whether an MSG is local.
- choice can be done in PTIME .
- A non-local choice MSG can be turned into a local choice MSG by adding synchronization messages.



REALIZING LOCAL CHOICE MSGS

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MSG G which is local choice is safely realizable with additional data (which is of size linear in G)

Proof let $G = (V, \rightarrow, v_0, F, \lambda)$ be a local choice MSG. We construct the MPA

$$A_G = ((A_p)_{p \in P}, \mathbb{D}, s_{in}, F')$$

$\downarrow$
 (s_p, Δ_p)

- first consider the local automata A_p (i.e., define s_p and Δ_p)
- define $\mathbb{D}$
- global initial state s_{in}
- the set of global accepting states F'

REALIZING A LOCAL CHOICE MSG

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- local choice: at every branch $v \in G$ there is a unique process p , say, such that on every path from v the unique minimal event occurs at p
- Idea of constructing an MPA:
 - process p determines the successor vertex of v ;
 - process p informs other processes about its decision by adding synchronization data to messages;
 - synchronization data ~~is~~ path from v to next branching vertex.

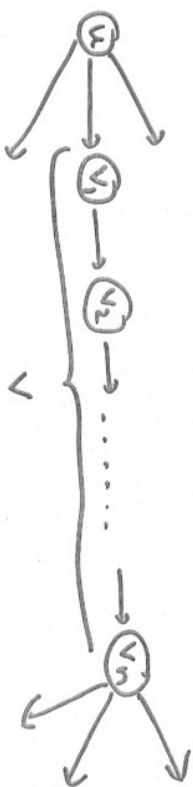
REALIZING A LOCAL CHOICE MSG

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Let $nbp : V \rightarrow V^*$ such that $nbp(v)$ is a ~~maximal~~ maximal non-branching path in $MSG G$ to which v belongs

$$nbp(v) = \begin{cases} v & \text{if } v \in F \text{ or } v \text{ is a branching vertex} \\ v_1 \dots v_n & \text{otherwise *} \end{cases}$$

*) where $v_i \in v$ for some i , $0 \leq i \leq n$, $v_n \in F$ or is a branching vertex, and v_1 is a direct successor of a branching vertex and $v_2, \dots, v_{n-1} \notin F$ and are non-branching



LOCAL AUTOMATA

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Local automaton A_p for process p is:

- $S_p = V \times E_p$, that is,

state = $\left(\begin{array}{l} \text{vertex } v, \\ \text{in } G \end{array} \right)$, all events that already occurred in $MSG \lambda(v)$ in E_p

More precisely:

$S_p = (v, I)$ with $I \subseteq E_p$ downward-closed wrt. $\leq_p$

(process order in $\lambda(v)$)

$e \leq_p e'$ and $e' \in I \implies e \in I$
in the $MSG \lambda(v)$

- Δ_p is defined by two inference rules:

$$(1) \frac{}{(u, I) \xrightarrow[e \in E_p]{\ell(e), m} (v, I \uplus \{e\})} \text{ with } m = nbp(v)$$

Note: since $I \uplus \{e\}$ is downclosed wrt. $\leq_p$, event e is enabled at process p . u_i

$$e \in E_p^w \cap \lambda(w) \quad \forall u_0 \dots u_n w \in \text{Path}(G) \quad \forall u_i: E_p = \emptyset$$

$$(2) \frac{(u, E_p^v) \xrightarrow[\ell(e), m]{\ell(e), m} (w, \{e\})}{(u, E_p^v) \xrightarrow[\ell(e), m]{\ell(e), m} (w, \{e\})} \quad \begin{array}{l} m = nbp(w) \\ v \neq w \end{array}$$

$\uparrow$... all events in $\lambda(v)$ at p has occurred

REMAINING COMPONENTS

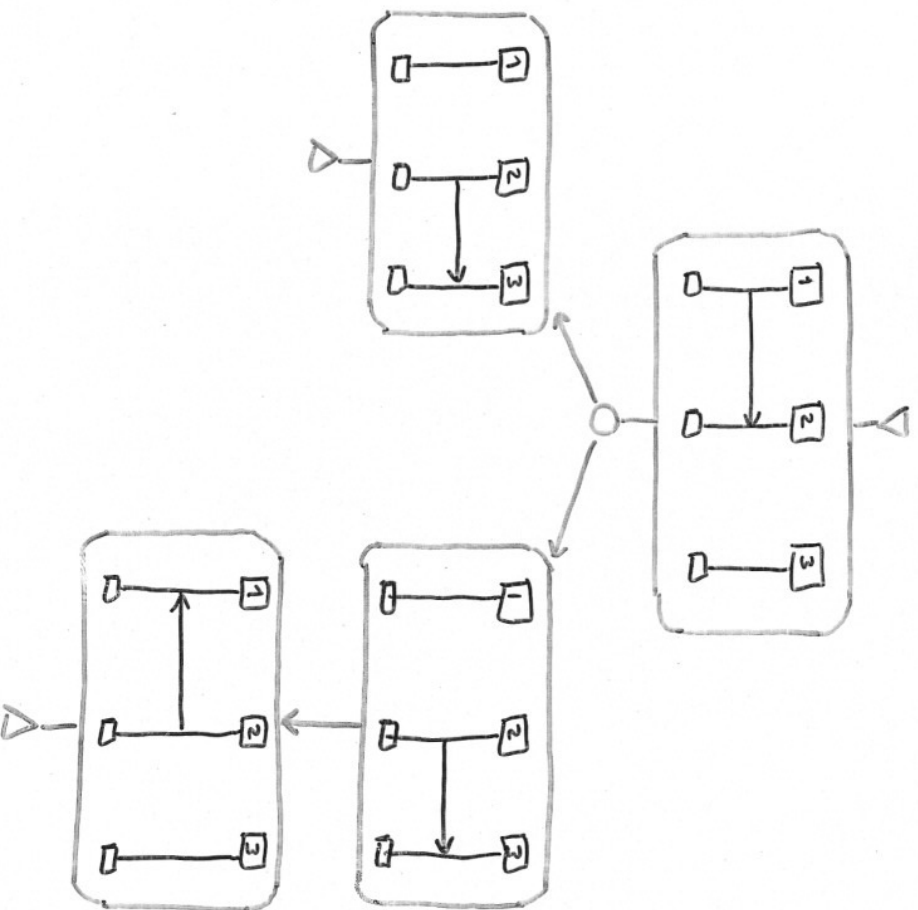
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- $ID = \{ \text{nbpf}(v) \mid v \in V \}$ set of maximal non-branching paths in MSG G
 - S_{in} , global initial state $= \{ (v_0, \emptyset) \}^n$ where $\# \text{ processes} = n$
 - Global final states $F' \subseteq \prod_{p \in P} S_p$ such that $(s_{p_1}, \dots, s_{p_n}) \in F'$ iff $\forall 0 < i \leq n$:
 $S_{p_i} = (v, O_p)$ with $O_p' \subseteq E_p'$ such that
 - (1) $v \in F$ and O_p'' contains a maximal event wrt. $\leq_p$ in $\text{MSC } \lambda(v)$
- or
- (2) $v \notin F$ and $\exists v' \in F$. $\pi = v \dots v'$ is a path in G and O_p'' contains a maximal event wrt. $\leq_p$ in $\text{MSC } \lambda(\pi)$.

EXAMPLE

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..... on the black board



SUMMARY OF MSC-PART

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- MSCs: scenario-based, graphical language
- Used in requirements engineering
- Standardized by ITU, UML,

- Formally: $MSC\ M = (P, E, \mathcal{E}, \ell, m, <)$

$< \subseteq ExE$ is a partial order ("visual order")
 $< = \bigcup_{p \in P} <_p \cup \{(e, m(e)) \mid e \in E\}$

+ FIFO property is guaranteed

- There is a one-to-one correspondence between MSCs and their linearizations

- M has a race if visual order $\neq$ possible order

Checking whether M has a race is in PTIME
(variant of Floyd-Warshall)

- Sets of MSCs can be conveniently described by Message Sequence Graphs

SUMMARY OF MSGs

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- An MSG is a digraph with a designated set of final vertices, and each vertex is labeled with an MSC.

- The MSC language of MSG G is given by:
 $L(G) = \{ M(\pi) \mid \pi \text{ is accepting path in } G \}$

- Checking whether an MSG has a race is undecidable.

- State space of an MSG is context-sensitive

- Checking whether MSG is local choice is in PTIME

- The decision problem "is $L(G_1) \cap L(G_2) = \emptyset$ " is undecidable.

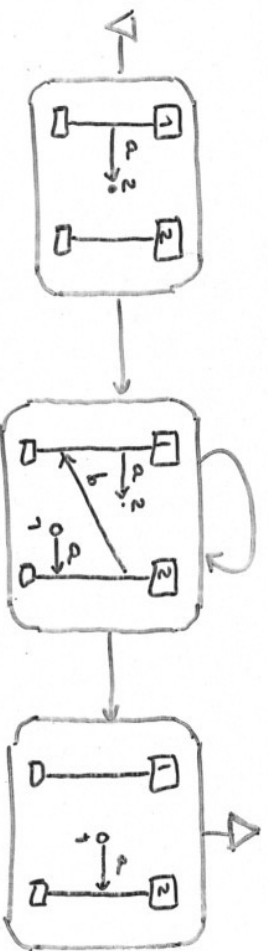
- There are (regular) MSCs that cannot be represented by an MSG

$\Rightarrow$ compositional MSGs (and MSCs)

SUMMARY OF CMSCs

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- A CMSC allows $m: E_i \rightarrow E_j$ to be partial
- A CMSC is like an MSG where vertices are labeled with CMSCs.



- Path π in CMSC G is safe if $M(\pi)$ is an MSC
- The existence of a safe path in G is undecidable ^{accepting}
- Checking whether all accepting paths in G are safe can be done in PTIME

SUMMARY OF MPAs

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- An MPA is a set of finite-state automata with a finite set of communication channels of unbounded capacity (but FIFO)
- The MSC language of MPA A is $L(A)$
- Checking whether $L(A) = \emptyset$ for MPA A is undecidable.
- MPA A is $\forall B$ -bounded if all its linearizations ($=$ runs) are B -bounded ($B \in \mathbb{N}$)
- MPA A is $\exists B$ -bounded if some of its runs are B -bounded ($B \in \mathbb{N}$)
- MPAs with $|D| = 1$ are less expressive than MPAs with $|D| > 1$.
- For every MPA A which is $\forall B$ -bounded: $\text{Lin}(A)$ is a regular (word) language

SUMMARY OF REALIZABILITY

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- MSG G is realizable if $L(G) = L(A)$ for some MPA A
- MSC language $L \subseteq \text{Act}^*$ is realizable iff $\forall w \in \text{Act}^*. (\forall p \in P. \exists v \in L. w \upharpoonright p = v \upharpoonright p) \rightarrow w \in L$.
- Checking whether L is realizable is coNP-complete
 $\Rightarrow$ this all refers to finite set of MSCs
- MSG G is safely realizable if it is realizable by a deadlock-free MPA
- MSC language $L \subseteq \text{Act}^*$ is safely realizable iff $\forall w \in \text{pref}(L). (\forall p \in P. \exists v \in L. w \upharpoonright p = v \upharpoonright p) \rightarrow w \in L$
and
 $\forall w \in \text{pref}(L). (\forall p \in P. \exists v \in \text{pref}(L). w \upharpoonright p = v \upharpoonright p) \rightarrow w \in \text{pref}(L)$
- Checking whether L is safely realizable can be done in PTIME

SUMMARY OF REGULARITY

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- MSG G is regular if $\text{Traces}(G)$ is a regular language
- Checking whether MSG G is regular is undecidable
- Checking "is regular $L \subseteq \text{Act}^*$ an MSC language" is decidable
- Any regular MSC language is realizable by a $\forall$ -bounded, deterministic MPA
- MSG G is communication-closed if for any loop in G its comm. graph is strongly connected
- G is communication-closed $\Rightarrow G$ is regular
- Checking realizability of a comm.-closed MSG is undecidable; safe realizability is ~~EXPTIME~~ EXPTIME complete
- A set $\mathcal{D}$ of MSCs is realizable iff there exists a connected regular expression α with $L(\alpha) = \mathcal{D}$