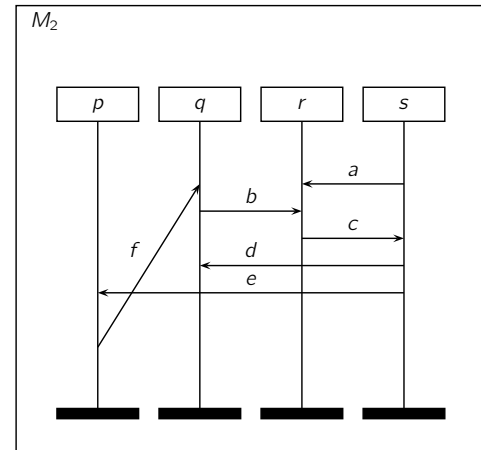
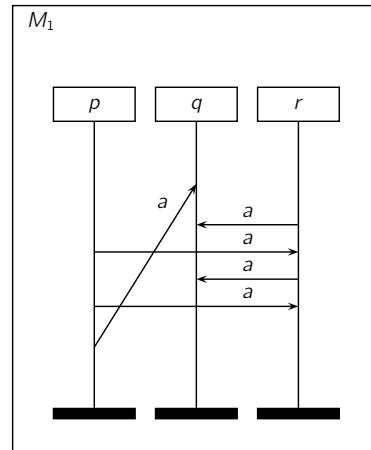


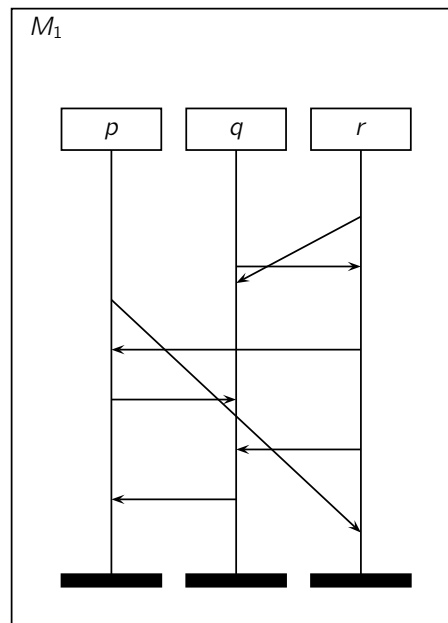
## Exercise 1 (Message Sequence Charts):

(4+2 Points)

- a) Let the following pictures  $M_1$ ,  $M_2$ , be given: Prove or disprove that  $M_1$  and  $M_2$  are MSCs.



- b) Does the following MSC have a race? Justify your answer.



## Exercise 2 (Concatenation):

(5 Points)

The *weak concatenation* of two MSCs  $M_1$  and  $M_2$  (with  $M_i = \langle \mathcal{P}_i, E_i, \mathcal{C}_i, \ell_i, m_i, <_i \rangle$  for  $i \in \{1, 2\}$ ) intuitively is realized by gluing the process lines together such that  $M_1$  is situated on top of MSC  $M_2$  (cf. Figure 1).

Define the so-called *strong concatenation*  $\cdot_s$  of two MSCs  $M_1$  and  $M_2$ , i.e., all events of MSC  $M_1$  have to be executed before the first event of  $M_2$  is executed. For this purpose determine a MSC  $M = M_1 \cdot_s M_2 = \langle \mathcal{P}, E, \mathcal{C}, \ell, m, < \rangle$ , that (in terms of  $M_1$  and  $M_2$ ) results from concatenating the two MSCs strongly.

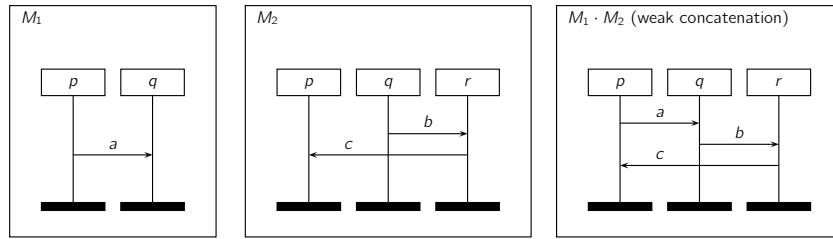


Abbildung 1: Two MSCs and their weak concatenation

### Exercise 3 (Prove or disprove):

(10 Points)

Formally prove or disprove the correctness of the following statements for MSGs (i.e.,  $M_i \in \mathbb{M}$ ,  $i \in \{1, 2, 3\}$ ):  
 (remember:  $| \hat{=}$  choice,  $\times \hat{=}$  (weak) sequence,  $*$   $\hat{=}$  iteration)

1.  $M_1 | M_2 = M_2 | M_1$
2.  $M_1 \times M_2 = M_2 \times M_1$
3.  $(M_1 \times M_2) \times M_3 = M_1 \times (M_2 \times M_3)$
4.  $(M_1 \times M_2) | M_3 = (M_1 | M_3) \times (M_2 | M_3)$
5.  $M_1^* | M_2^* = (M_1 | M_2)^*$