

## Introduction to Model Checking Summer term 2007

### – Series 5 –

Hand in on May 11 before the exercise class.

#### Exercise 1

(2 + 2 points)

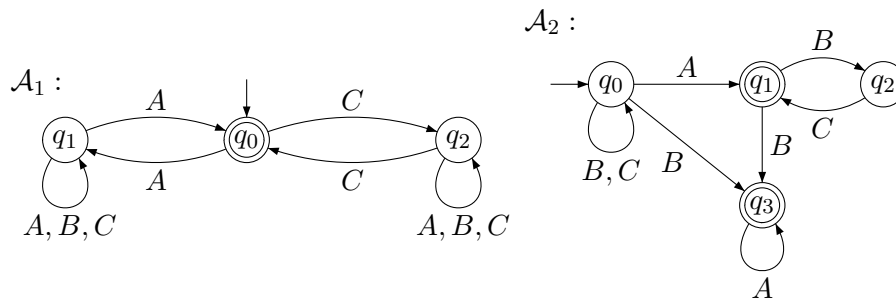
Find nondeterministic Büchi automata that accept the following  $\omega$  regular languages:

- a)  $L_1 = \{\sigma \in \{A, B\}^\omega \mid \sigma \text{ contains } ABA \text{ infinitely often, but } AA \text{ only finitely often}\}$
- b)  $L_2 = \mathcal{L}_\omega((AB + C)^*((AA + B)C)^\omega + (A^*C)^\omega)$

#### Exercise 2

(1 + 2 points)

Consider the following NBA  $\mathcal{A}_1$  and  $\mathcal{A}_2$  over the alphabet  $\Sigma = \{A, B, C\}$ :



Find  $\omega$  regular expressions for the languages accepted by  $\mathcal{A}_1$  and  $\mathcal{A}_2$ , respectively.

#### Exercise 3

(4 points)

Prove or disprove the following equivalences for  $\omega$ -regular expressions:

- a)  $(E_1 + E_2).F^\omega \equiv E_1.F^\omega + E_2.F^\omega$
- b)  $E.(F_1 + F_2)^\omega \equiv E.F_1^\omega + E.F_2^\omega$
- c)  $E.(F.F^*)^\omega \equiv E.F^\omega$
- d)  $(E^*.F)^\omega \equiv E^*.F^\omega$

Here,  $E, E_1, E_2, F, F_1, F_2$  denote regular expressions with  $\varepsilon \notin \mathcal{L}(F) \cup \mathcal{L}(F_1) \cup \mathcal{L}(F_2)$ .

#### Exercise 4

(4 points)

Show that the class of languages accepted by DBA is not closed under complementation.