

## Introduction to Model Checking Winter term 2011/2012

### – Series 12 –

Hand in on January 25<sup>th</sup> before the exercise class.

#### Exercise 1

(4 points)

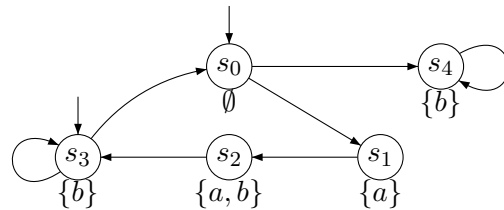
Consider the following CTL formulas and the transition system  $TS$  outlined on the right:

$$\Phi_1 = \forall(aUb) \vee \exists\bigcirc(\forall\Box b)$$

$$\Phi_2 = \forall\Box\forall(aUb)$$

$$\Phi_3 = (a \wedge b) \rightarrow \exists\Box\exists\bigcirc\forall(bWa)$$

$$\Phi_4 = (\forall\Box\exists\Diamond\Phi_3)$$



Give the satisfaction sets  $Sat(\Phi_i)$  and decide whether  $TS \models \Phi_i$  holds ( $1 \leq i \leq 4$ ).

#### Exercise 2

(2 points)

Transform the CTL-formula  $\Phi = \neg\forall\Diamond(\forall(\forall\Box b) \cup (\forall\bigcirc a))$  into an equivalent CTL-formula in

- (a) existential normal form and
- (b) positive normal form.

#### Exercise 3

(4 points)

Consider the following CTL-formulas

$$\Phi_1 = \exists\Diamond\forall\Box c \quad \text{and} \quad \Phi_2 = \forall(aU\forall\Diamond c)$$

and the transition system outlined on the right. Decide whether  $TS \models \Phi_i$  for  $i = 1, 2$  using the CTL model checking algorithm from the lecture. Sketch its main steps!

