

Modeling Concurrent and Probabilistic Systems

Summer Term 09

— Series 3 —

Hand in until May 20 before the exercise class.

Exercise 1

(3 + 1 points)

In analogy to the buffer, this exercise deals with the *semaphore* data structure which can be regarded as a buffer for identical entries.

a) An n -ary semaphore ($n \geq 1$) is given by the following specification:

$$\begin{aligned} Sem_0^n(get, put) &= get.Sem_1^n(get, put) \\ Sem_k^n(get, put) &= get.Sem_{k+1}^n(get, put) + put.Sem_{k-1}^n(get, put) \quad (0 < k < n) \\ Sem_n^n(get, put) &= put.Sem_{n-1}^n(get, put). \end{aligned}$$

Prove that it can also be specified by composing n parallel instances of a unary semaphore:

$$\begin{aligned} S^n(get, put) &= \underbrace{S_0(get, put) \parallel S_0(get, put) \parallel \dots \parallel S_0(get, put)}_{n \text{ times}} \\ S_0(get, put) &= get.S_1(get, put) \\ S_1(get, put) &= put.S_0(get, put). \end{aligned}$$

To this aim, show that $Sem_0^n \sim S^n$ by constructing an appropriate strong bisimulation relation.

b) Show that the two variants of the two place buffer given in the lecture are not strongly bisimilar.

Exercise 2

(2 points)

Prove or disprove the following strong bisimulation equivalences between process terms:

- a) $P + nil \sim P$
- b) $P \parallel (Q \parallel R) \sim (P \parallel Q) \parallel R$

Exercise 3

(3 points)

Prove that it is undecidable whether a given CCS process definition induces a finite or an infinite transition system.

Hint: a turing tape can be simulated by means of two stacks.