

## 1. Exercise sheet *Semantics and Verification of Software 2007*

Due to Wed., 18 April 2007, *before* the exercise course begins.

### Exercise 1.1:

In this exercise we will discuss *alternative evaluation strategies* for Boolean expressions.

- (a) *Sequential evaluation*: Define operational rules for Boolean expressions of the form  $b_1 \wedge b_2$  and  $b_1 \vee b_2$  which do *not* evaluate  $b_2$  provided that the value of  $b_1$  is **false** (**true**, respectively). (In these cases, the value of  $b_2$  does not contribute to the overall result.)
- (b) *Parallel evaluation*: Define operational rules which evaluate a Boolean expression of the form  $b_1 \vee b_2$  to **true** if  $b_1$  or  $b_2$  evaluates to **true**, and which do not evaluate  $b_2$  ( $b_1$ , respectively) in this case.

### Exercise 1.2:

In the lecture we have defined a so-called *bigstep semantics* for expressions, i.e., a relation  $\rightarrow \subseteq (AExp \cup BExp) \times \Sigma \times (\mathbb{Z} \cup \mathbb{B})$  which yields the value of an expression within one step:  $\langle (3 + 3) * (9 - 2), \sigma \rangle \rightarrow 42$ . (Thus the intermediate results of the computation are “hidden” in the derivation tree.)

Alternatively it is possible to explicitly represent the intermediate steps by defining a *single-step semantics*:  $\langle (3 + 3) * (9 - 2), \sigma \rangle \rightarrow \langle 6 * (9 - 2), \sigma \rangle \rightarrow \langle 6 * 7, \sigma \rangle \rightarrow \langle 42, \sigma \rangle \rightarrow 42$ . Give a complete specification of the single-step relation

- (a)  $\rightarrow_1^a \subseteq (AExp \times \Sigma) \times (AExp \times \Sigma \cup \mathbb{Z})$  for arithmetic expressions and
- (b)  $\rightarrow_1^b \subseteq (BExp \times \Sigma) \times (BExp \times \Sigma \cup \mathbb{B})$  for Boolean expressions.